

Block Cipher Modes

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Lecture 3

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Topics for Today

- Block Cipher Modes:
 - ECB
 - CBC
 - OFB
 - CTR
 - GCM
- Other ciphers and modes
- Sources: HAC 7.2.2, 9.1-9.4, 12.6.1

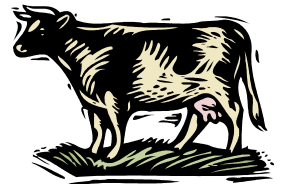
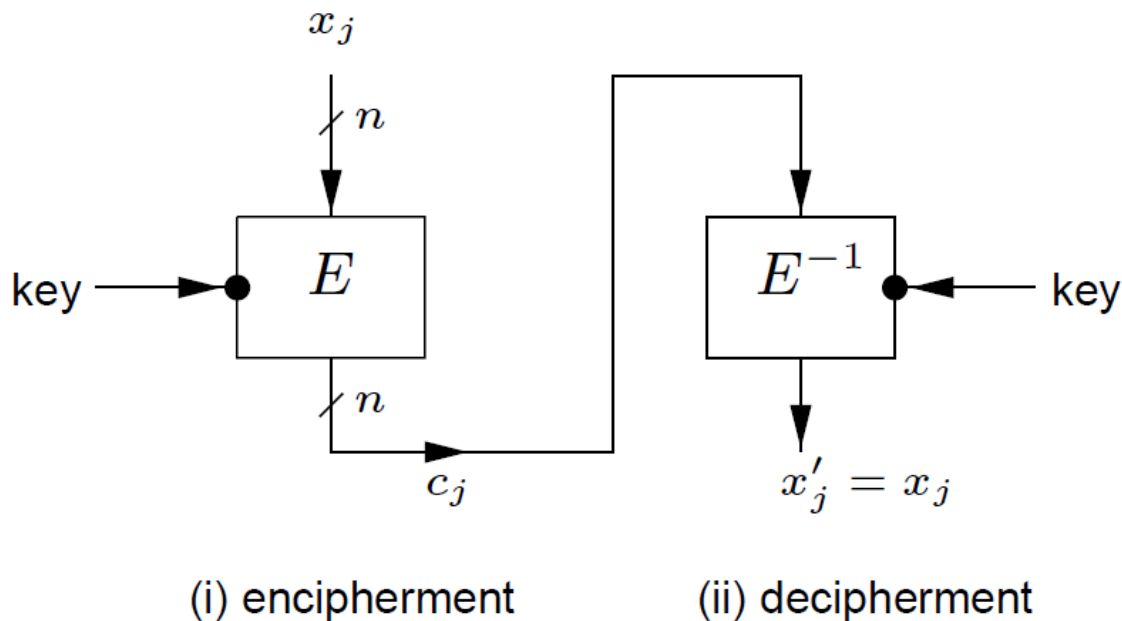
Block Cipher Modes

What do we do with a block cipher of size n if the message size is greater than n ?

Electronic Code Book (ECB)

- Simplest idea: Break the message into n bit blocks and encipher each one independently

a) Electronic Codebook (ECB)



ECB Properties

Identical plaintext blocks

- Under the same key result in identical ciphertext
- Preserves patterns in messages

No Chaining Dependencies

- Blocks are enciphered independently of all other blocks.
- Re-ordering ciphertext blocks results in corresponding re-ordered plaintext blocks

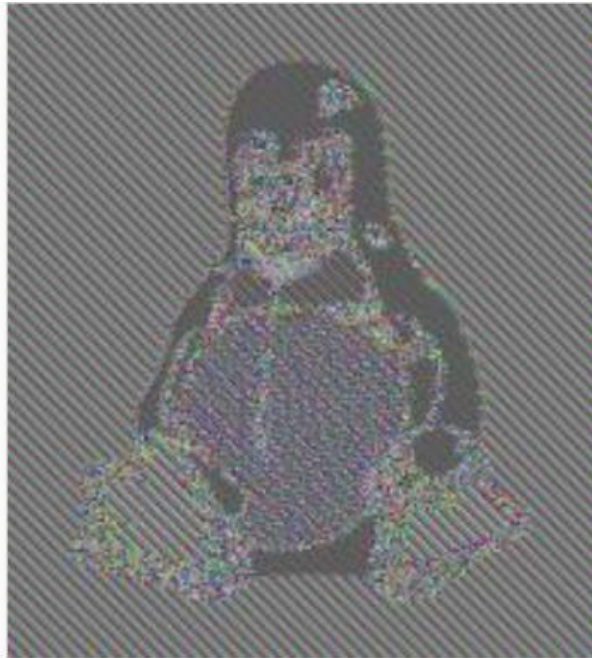
Error propagation

- One or more bit errors in a single ciphertext block affect decipherment of that block only

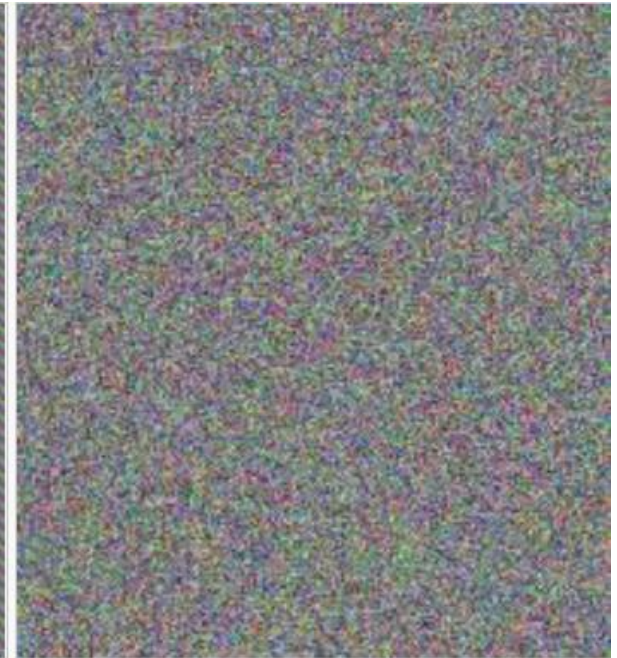
ECB Visualized



Original image



Encrypted using ECB mode



Modes other than ECB result in pseudo-randomness

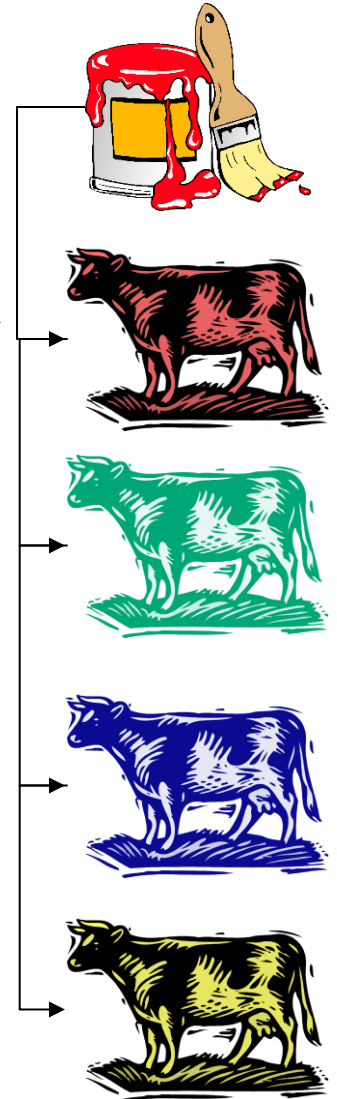
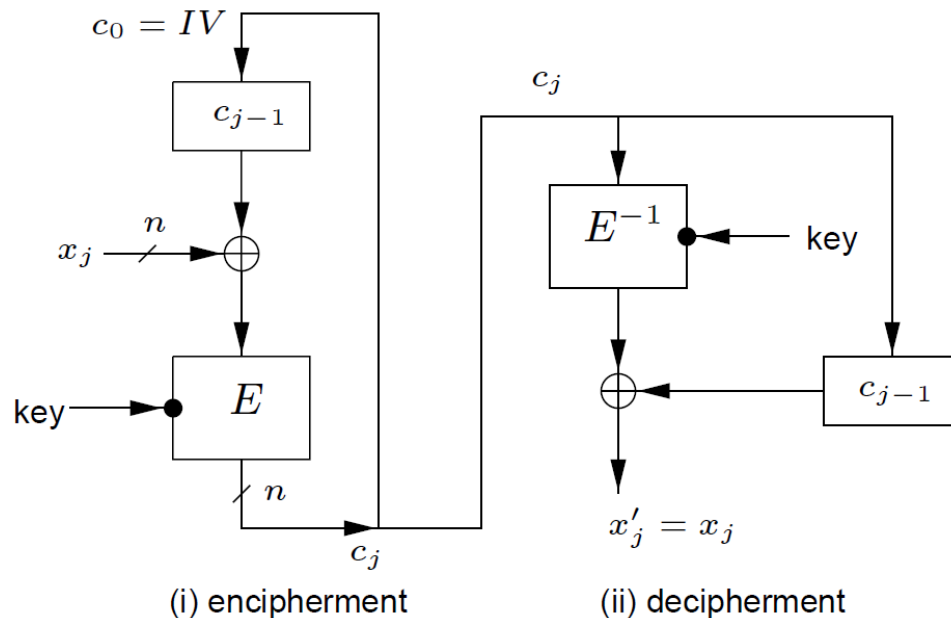
So Far

- Block Cipher Modes:
 - ECB
 - CBC
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- Other ciphers and modes

Cipher Block Chaining (CBC)

- Chain each block based on the previous one
 - Introduce randomness to each block
 - Introduce dependencies in the message
- Use an Initialization Vector (IV) for the first block

b) Cipher-block Chaining (CBC)



CBC Properties

Identical plaintexts

- Identical ciphertext blocks result when the same plaintext is enciphered under the same key and IV

Chaining dependencies

- Chaining mechanism causes ciphertext c_j to depend on x_j and all preceding plaintext blocks
- Entire dependency on preceding blocks is, however, contained in the value of the previous ciphertext block.

CBC Properties

Error propagation

- A single bit error in ciphertext block c_j affects decipherment of blocks c_j and c_{j+1} (since x_j depends on c_j and c_{j-1}).
- Block x'_j recovered from c_j is typically totally random (50% in error)
- The recovered plaintext x'_{j+1} has bit errors precisely where c_j did.
- Thus an adversary may cause predictable bit changes in x_{j+1} by altering corresponding bits of c_j

Error recovery

- CBC mode is self-synchronizing in the sense that if an error (including loss of one or more entire blocks) occurs in block c_j but not c_{j+1} , c_{j+2} is correctly decrypted to x_{j+2}

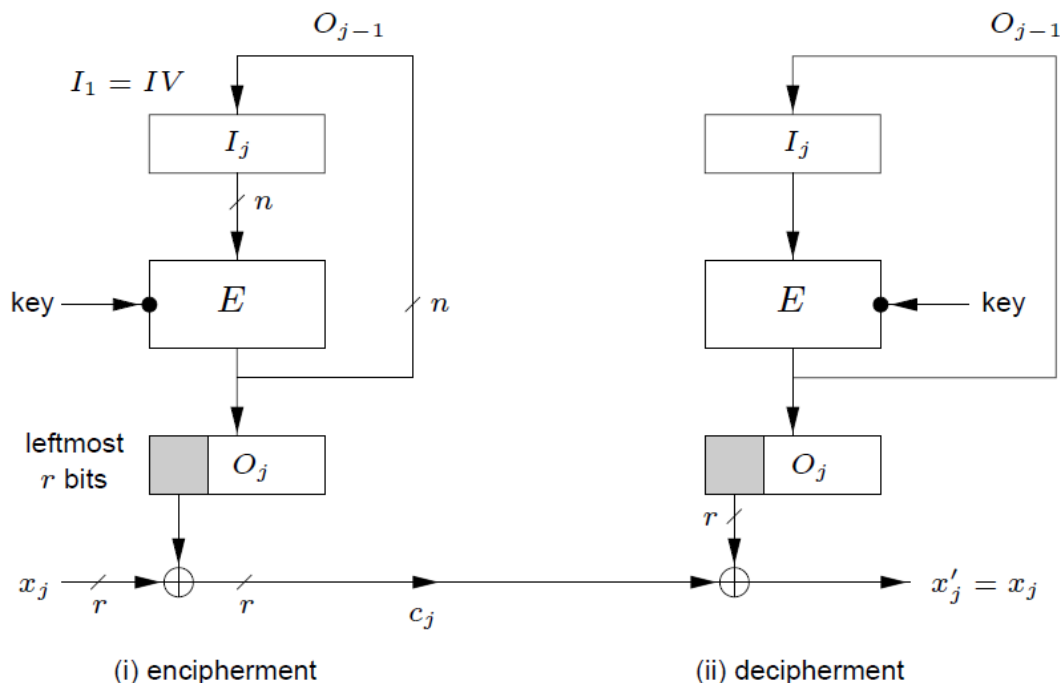
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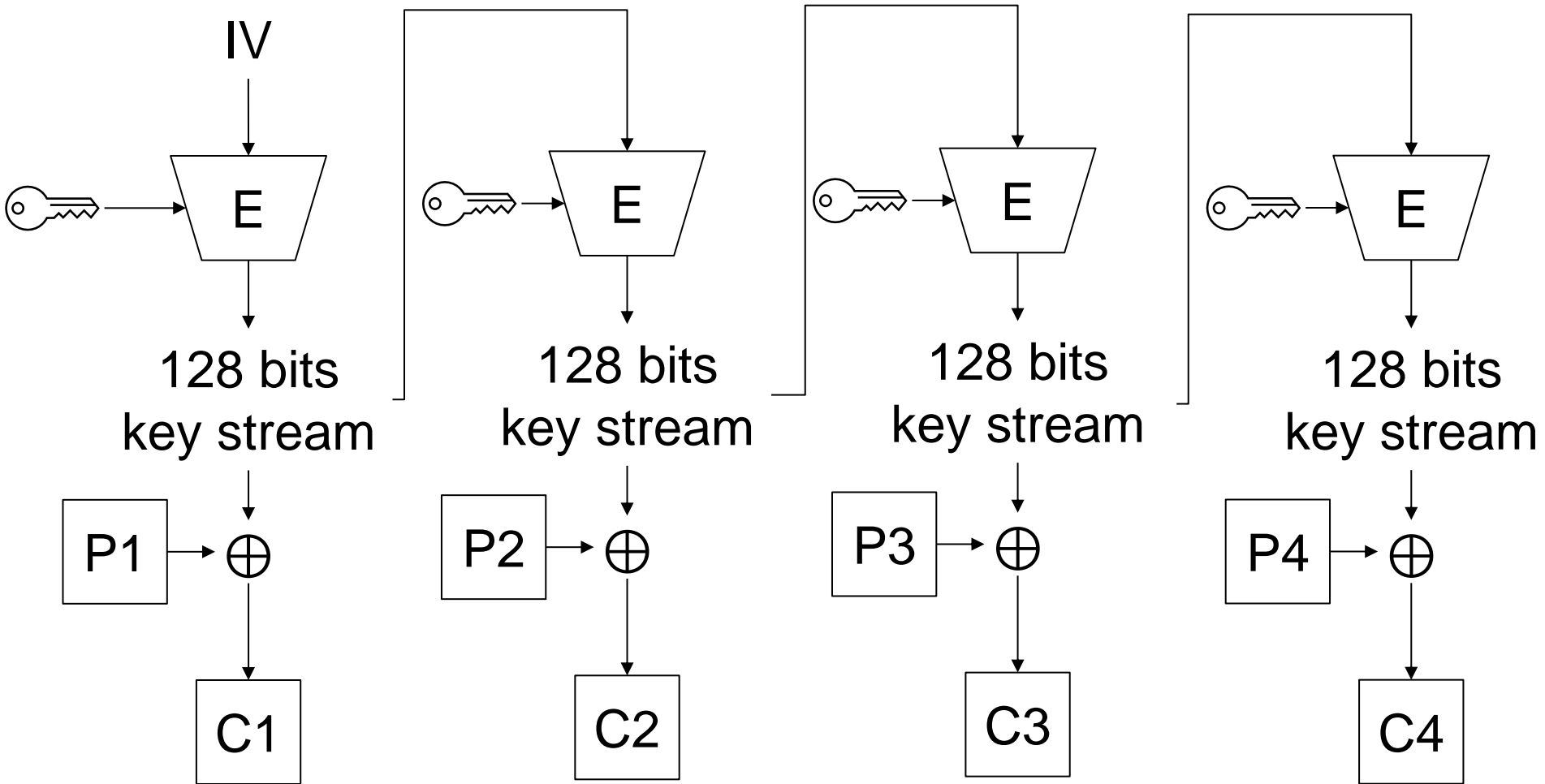
Output Feedback Mode (OFB)

- Make the encryption solely dependent on the IV and key
 - Remove all chaining dependencies
- Creates a stream cipher from a block cipher
 - No need for a separate decryption algorithm

d) Output feedback (OFB), r -bit characters/ n -bit feedback



OFB Operations

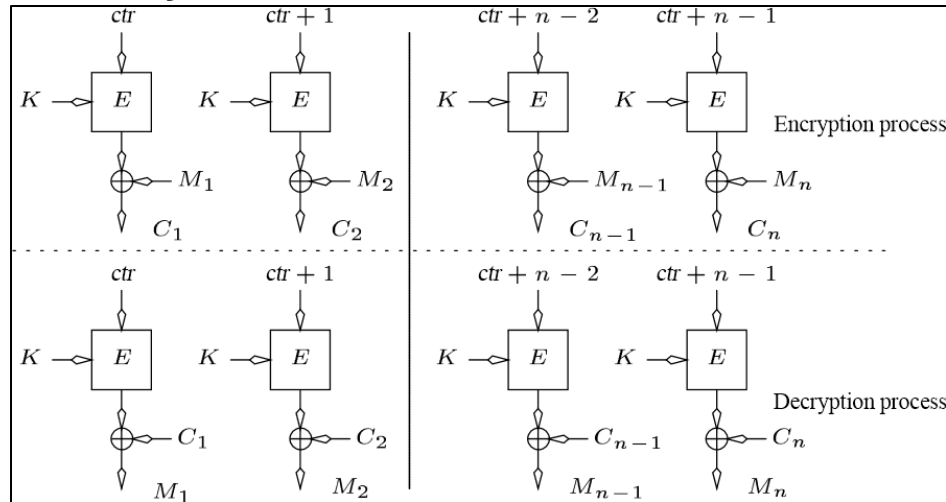


OFB Properties

- **Identical plaintexts:** identical ciphertext blocks result when the same plaintext is enciphered under the same key and IV .
 - The IV must be changed if the key is to be reused.
- **Error Propagation:** One or more bit errors in any ciphertext character c_j affects the decipherment of only that character in the precise bit position(s) c_j is in error, causing the corresponding plaintext bit(s) to be complemented.
- **Error recovery:** OFB recovers from ciphertext bit errors, but can't self-synchronize after loss of ciphertext bits, which destroys alignment
- **Throughput:** Since keystream is independent of plaintext or ciphertext, it may be pre-computed.

Counter Mode (CTR)

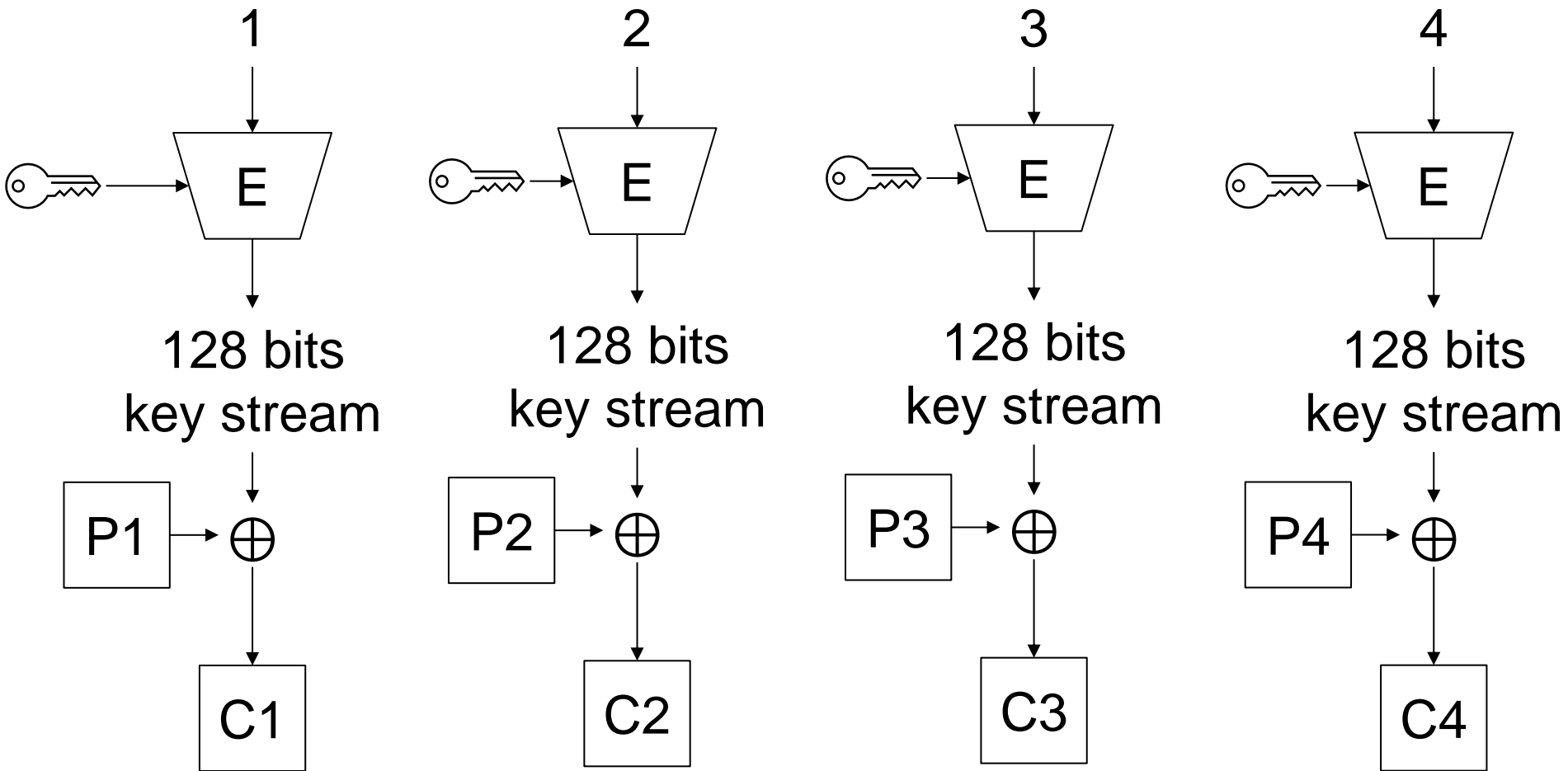
- A simplification of OFB in which $IV = 0$ and the input blocks $I_{j+1} = I_j + 1$ rather than using feedback



Properties:

- Avoids problem of repeating IV (if encrypting IV many times eventually leads to it recurring)
- Allows random access decryption
 - Ciphertext block i need not be decrypted to decrypt block $i + 1$

CTR Operations

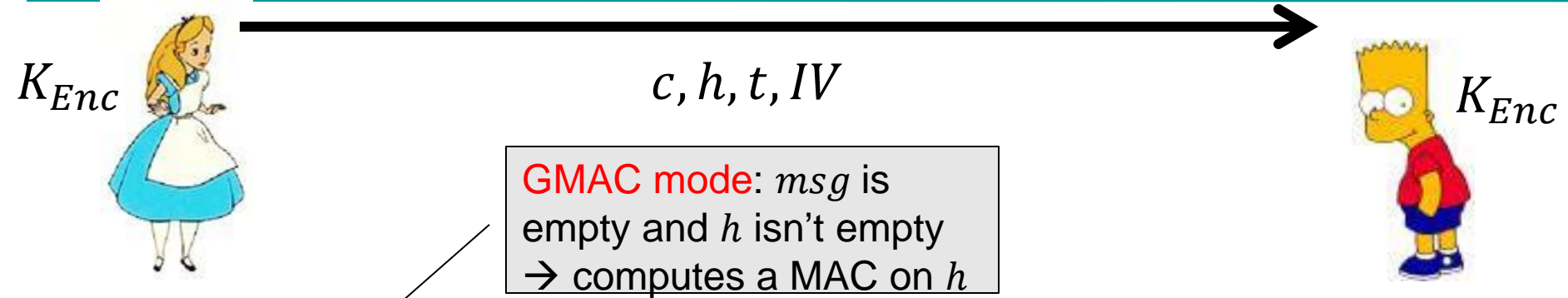


A look ahead

- Modern cipher modes combine encryption with authentication:
 - *Authenticated Encryption with Associated Data (AEAD)*
- Later we'll talk about **Message Authentication Codes (MAC)** in general
 - *HMAC*
 - *Encrypt and then MAC*
 - *Galois Counter Mode (GCM)*



Using GCM



1. Wants to send msg with secrecy and integrity
2. Wants to send h with integrity only
3. Sets Additional Authentication Data $AAD = h$
4. Chooses tag length len (128 bits)
5. Chooses unique IV (96 bits)
6. GCM Encrypts $(c, t) = E_{K_{Enc}, AAD, IV}\{msg\}$
GCM gives two outputs (t is len bits)

7. GCM Decrypts

$$p = D_{K_{Enc}, h, t, IV}\{c\}$$

8. If D doesn't return FAIL:
 $p == msg$ and unchanged
 h is unchanged

GCM Notes (from NIST)

Uniqueness of IV is critical

Using same IV twice with same key leads to compromise

- Using 96 bit IV is recommended, longer or shorter ones are hashed

Short tags are bad: 128 bits is recommended.

- 32 bit tags can only be used for **tens** of bytes per key
- 64 bit tags can only be used for **millions** of bytes per key (few *MBs*)

Don't use a key **more than** 2^{32} times no matter what

GCM can encrypt up to **64 GB** per message securely

Other Ciphers and Modes

Block Ciphers

- Speck (IoT)
- Simon (IoT)
- CAST-256
- Camellia
- Other Modes:
 - Cipher Feedback (CFB)
 - CCM (Counter with CBC-MAC)
 - Ciphertext Stealing (CTS)

Stream Ciphers

- ChaCha20 / Salsa20
- HC-256

Conclusion

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